

Introduction

Definition. Template matching can be defined as a method of parameter estimation, to choose the template position that minimizes a similarity measure between a discrete function $T_{x,y}$ (taking values in a window W) and an image I e.g. with sum of squared differences

$$\min e = \sum_{(i,j) \in I} \sum_{(x,y) \in W} (I_{x+i,y+j} - T_{x,y})^2$$

The template matching problem is concerned with different parameters

- n the size of the template
- $O(f(n))$ the computation cost of the similarity measure
- m the image size
- θ_k the orientation search parameter
- S_k the scale search parameter
- p the template number

The combination of the parameters m, θ_k, S_k, p is the search space, the computation cost depends on the search space dimension and the used similarity measure $O(f(n))$

Binary Similarity Measures

Binary similarity (or dissimilarity) measures can be applied to binary images by requiring significantly less resource comparing to the ones working in the gray domain.

We consider X, Y two n -dimensional binary vectors

$X = (x_1, \dots, x_m, \dots, x_n)$ is one of the templates X_1, \dots, X_C

$Y = (y_1, \dots, y_m, \dots, y_n)$ is the image to compare

$$\delta_m(u, v) = \begin{cases} 1 & \text{if } x_m = u, y_m = v \\ 0 & \text{otherwise} \end{cases}$$

		v	
		0	1
u	0	n_{00} negative matches	n_{01} missmatches
	1	n_{10} missmatches	n_{11} positive matches

$$n_{uv} = \sum_{m=1}^n \delta_m(u, v)$$

Based on $n_{00}, n_{11}, n_{10}, n_{01}$, **76 binary similarity measures** $S(X, Y)$ are defined in the literature with close relationships. In DIA, common measures includes those of Table I

Measure	$S(X, Y)$	Range
Inner Product (IP)	n_{11}	$[0, +\infty[$
Jaccard and Needham (Jaccard)	$\frac{n_{11}}{n_{11} + n_{10} + n_{01}}$	$[0, 1]$
Dice (DICE)	$\frac{2n_{11}}{2n_{11} + n_{10} + n_{01}}$	$[0, 0.5]$
Russel-Rao (RUSS)	$\frac{n_{11}}{n}$	$[0, 1]$
Kulzinsky (KUL)	$\frac{n_{11}}{n_{10} + n_{01}}$	$[0, +\infty[$
Hamming (Hamming)	$n_{11} + n_{00}$	$[0, +\infty[$
Sokal and Michner (SM)	$\frac{n_{11} + n_{00}}{n}$	$[0, 1]$
Rogers and Tanimoto (RT)	$\frac{n_{11} + n_{00}}{n_{11} + n_{00} + 2(n_{10} + n_{01})}$	$[0, 1]$
Correlation (CORR)	$\frac{n_{11}n_{00} - n_{10}n_{01}}{\sqrt{n_{1x}n_{0x}n_{x1}n_{x0}}}$	$[-1, 1]$
Yule and Kendall (Yule)	$\frac{n_{11}n_{00} - n_{10}n_{01}}{n_{11}n_{00} + n_{10}n_{01}}$	$[-1, 1]$

Table I. COMMON BINARY SIMILARITY MEASURES IN DIA

Where $n_{ix} = n_{i0} + n_{i1}$, $n_{xi} = n_{0i} + n_{1i}$, $n = n_{ix} + n_{xi}$

Weighting is presented as very effective for boosting classification performance with negative matches i.e. '0' provides less information of separability than '1'.

We can define a weighted version for each dissimilarity measure by weighting n_{00} with $\beta (0 \leq \beta \leq 1)$

The IP, Jaccard, DICE, RUSS, and KUL are independent of n_{00} .

Optimal template matching

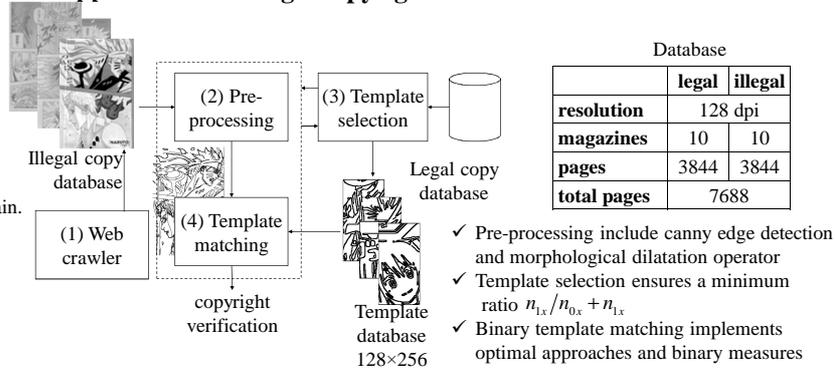
Definition. Optimal or Full-Search (FS) template matching scans the entire image and evaluates the similarity between the pattern and an area.

Method	Complexity	Coding	K=1	K=2	K≥3
Brute-force	$O(MNmn)$	integer			
FFT	$K \times O(M^2 \log_2 M^*)$	float	IP, RUSS, Ham, SM	Jaccard, Dice, KUL, RT	Yule, CORR
Bitwise operator	$K \times O(MNr)$	boolean	IP, RUSS, Ham, SM, RT,	Jaccard, Dice,	Yule, CORR

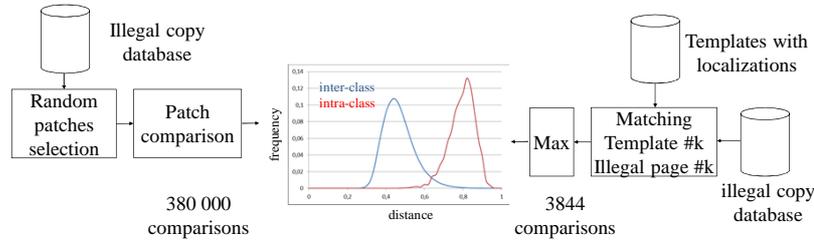
with MN and mn the image/ROI and template size respectively, M^* is M padded of the template size and round to a power of two, $r = \min(m, n)$

K depends of the distance computation

Application to Manga Copyright Protection



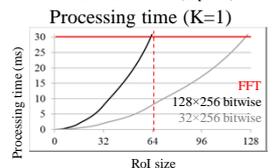
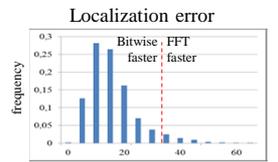
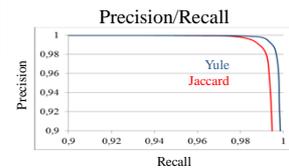
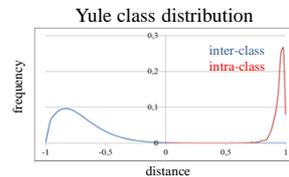
Binary similarity measure characterization can be expressed as an inter-class intra-class discrimination problem,



The Bhattacharyya coefficient measures the amount of overlap between two probability distributions $p(x), q(x)$

$$BC(q, p) = \sum_{x} \sqrt{p(x)q(x)}$$

	$BC(p, q)$	
	$\beta = 1$	$\beta = n_{11}/n_{00}$
Jaccard	0,01614	
Dice	0,01857	
Russ	0,25975	
Yule	0,00926	0,00224
RT	0,16604	0,01641
SM	0,16898	0,25461



Conclusion and perspectives

- ✓ Template matching is a good candidate for copyright verification supporting skew distortion, image shifting, scale approximation, compression & digitalization artifacts, scalable recognition.
- ✓ With a suitable selection of the distance and the template size, copyright verification problem is almost separable (near to a 1/1 Precision/Recall) on medium resolution images (128 dpi).
- ✓ Fast and optimal template matching can be achieved in some ten ms from regions of interest of 64x64 to 128x128 sizes, fitting with the localization errors, using a priori positions of templates.
- ✓ Major time improvement could be obtained with non-optimal approaches and template pruning strategies.