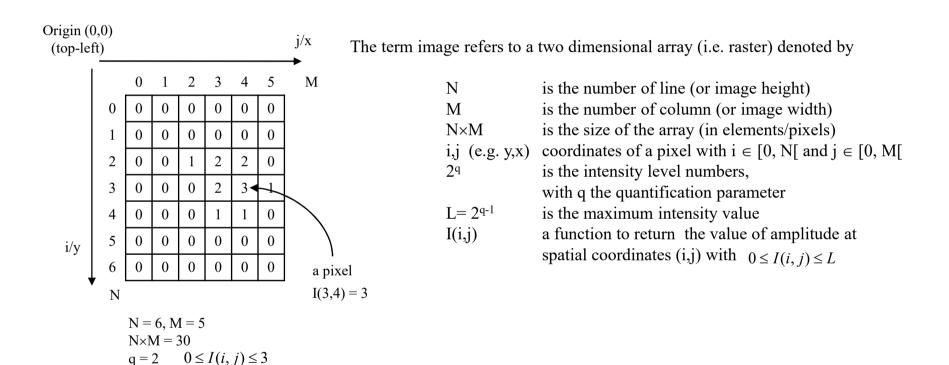
Image processing "Digital image modeling"

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Lecture available at http://mathieu.delalandre.free.fr/teachings/image.html

- 1. Representing digital image
- 2. Sampling and quantization
- 3. Color spaces
- 4. Relationships between pixels

Representing digital image (1)



Representing digital image (2)

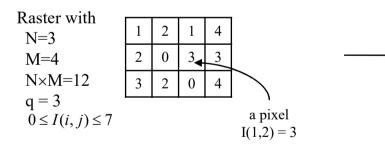
The histogram of a digital image is a representation of its intensity distribution such as

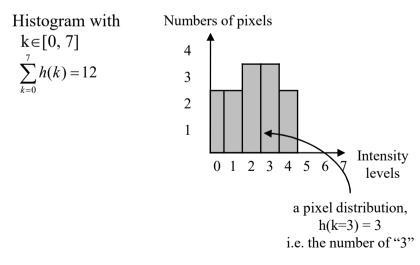
The image

I(i,j) = v	is a discrete function
i,j	the coordinates of a pixel
i ∈ [0, N[and $j \in [0, M[$
V	is the pixel intensity value with
	$0 \le v \le L$
M×N	is the size of the array (in pixels)

The histogr	am
$h(k) = n_k$	is a discrete function
k	the intensity value
k∈[0, L]	is the intensity level range
n _k	is the number of pixels in
L	the image of intensity k
$\sum_{k=0} h(k) = N$	$\times M$

e.g.





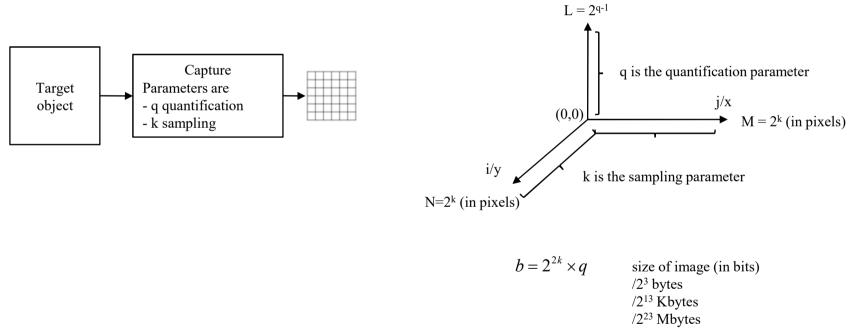
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Sampling and quantization (1)

To be suitable for computer processing digital image are first captured (camera, digitized, screenshot ...) both spatially and in amplitude

Specification of amplitude is called quantification

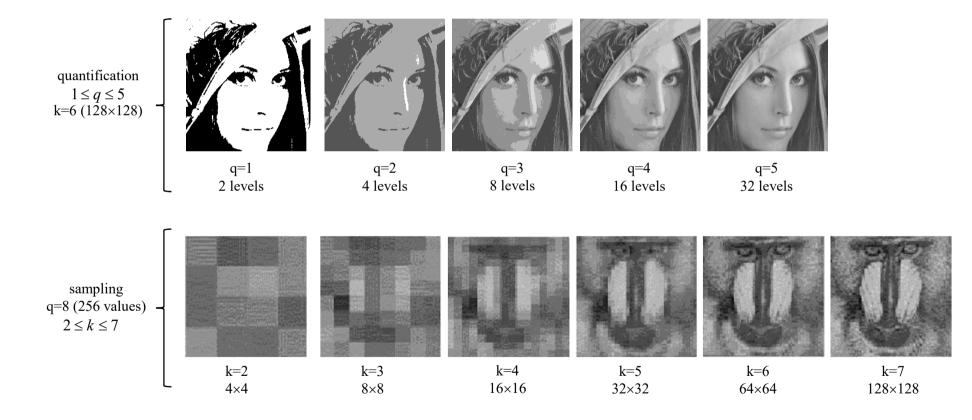
Specification of spatial coordinate is called sampling



etc.

Sampling and quantization (2)

Quantification and sampling parameters impact the image quality, they must be set considering the image content.



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Color spaces (1)

Quantification specifies the maximum number of possible amplitude values, correspondence between these values and colors is ensured by a color space.

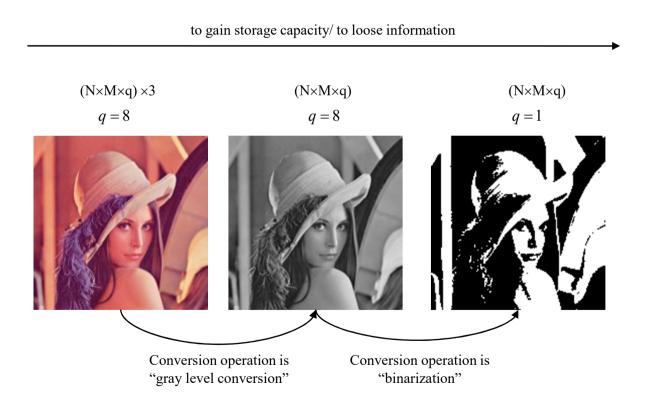
	q	- h h-	color codes					
	per channel	channels	black	white	red	blue	green	
		-		-			-	_
binary "miniswhite"	1	Ø	1	0	Ø	Ø	Ø	
binary "minisblack"	1	Ø	0	1	Ø	Ø	Ø	
				-	-	-	-	_
gray level	8	Ø	0	255	Ø	Ø	Ø	
								(G)reen (R)ed
		R	0	255	255	0	0	(O)reen
RGB	8 (to 24)	G	0	255	0	255	0	
		В	0	255	0	0	255	
								(B)lue
		С	255	0	0	255	255	(C)yan (M)agenta
СМУ	8 (to 24)	М	255	0	255	255	0	
		Y	255	0	255	0	255	

Others are at the corner: YIQ, HSV, etc.



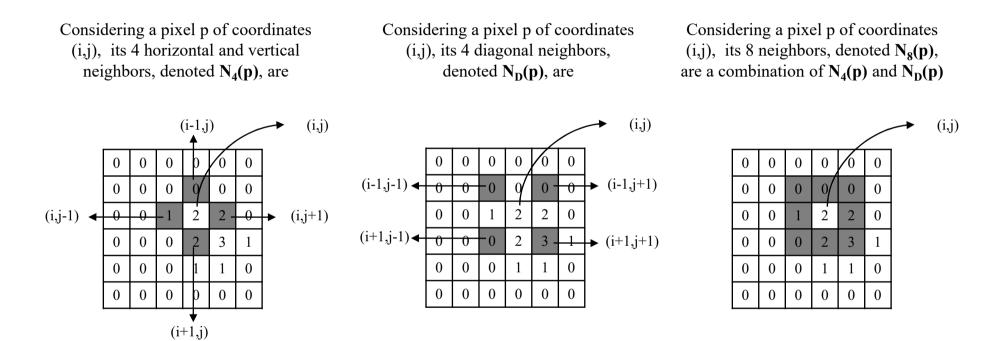
Color spaces (2)

To convert color space is a tradeoff between preserving information and to gain storage capacity.



- 1. Representing digital image
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Relationships between pixels (1)



Considering two pixels, p of coordinates	
(i,j) and q of coordinates (u,v)	

p and q are 4-adjacent if	$q \in N_4(p)$ and $p \in N_4(q)$
p and q are 8-adjacent if	$q \in N_8(p)$ and $p \in N_8(q)$

Relationships between pixels (2)

Considering the three pixels

- p of coordinates (i,j)

- q of coordinates (u,v)

- z of coordinates (x,y)

We define a relation D between p,q and z as distance if

(i)	$D(p,q) \ge 0$	non-negativity
(ii)	D(p,q) = 0 if $p = q$	reflexivity
(iii)	D(p,q) = D(q,p)	commutativity
(iv)	$D(p,z) \le D(q,p) + D(q,z)$	triangle inequality

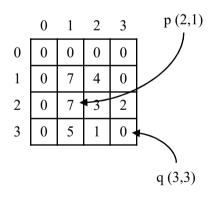
Example

Definitions

The Euclidean distance is defined as

 $D_{e}(p,q) = \left[(i-u)^{2} + (j-v)^{2} \right]^{\frac{1}{2}}$

$$D_e(p,q) = \left[(2-3)^2 + (1-3)^2 \right]^{\frac{1}{2}} = \sqrt{1+4} = \sqrt{5}$$



The city-block distance is defined as

$$D_4(p,q) = |i-u| + |j-v| \qquad D_4(p,q) = |2-3| + |1-3| = 1 + 2 = 3$$

The chessboard distance is defined as

$$D_8(p,q) = \max(|i-u|, |j-v|) \qquad D_8(p,q) = \max(|2-3|, |1-3|) = \max(1,2) = 2$$

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Relationships between pixels (3)

Considering the three pixels

- p of coordinates (i,j)

- q of coordinates (u,v)

- z of coordinates (x,y)

We define a relation D between p,q and z as distance if

(i)	$D(p,q) \ge 0$	non-negativity
(ii)	D(p,q) = 0 if $p = q$	reflexivity
(iii)	D(p,q) = D(q,p)	commutativity
(iv)	$D(p,z) \le D(q,p) + D(q,z)$	triangle inequality

Definitions

The Euclidean distance is defined as

$$D_e(p,q) = \left[(i-u)^2 + (j-v)^2 \right]^{\frac{1}{2}}$$

$\sqrt{8}$	$\sqrt{5}$	2	$\sqrt{5}$	$\sqrt{8}$
$\sqrt{5}$	$\sqrt{2}$	1	$\sqrt{2}$	√5
2	1	р	1	2
$\sqrt{5}$	$\sqrt{2}$	1	$\sqrt{2}$	$\sqrt{5}$
10	12	-	12	

р

The city-block distance is defined as

$$D_4(p,q) = |i-u| + |j-v|$$

The chessboard distance is defined as

$$D_8(p,q) = \max(|i-u|, |j-v|)$$

2	2	2	2	2
2	1	1	1	2
2	1	р	1	2
2	1	1	1	2
2	2	2	2	2

Distance maps of pixel p at coordinates (i,j)